

Complex Numbers

WS

Express as a product of a real number and i

1. $\sqrt{-9}$

2. $\sqrt{-49}$

3. $-2\sqrt{-1}$

4. $\sqrt{-\frac{4}{9}}$

Simplify

5. $\sqrt{-50} + \sqrt{-32} - \sqrt{-8}$

6. $\sqrt{9} \cdot \sqrt{-49}$

7. $(7 + 2i) - (4 - 3i)$

8. $(3 - 2i) + (9 - 4i)$

9. $2i(3 + 5i)$

10. $(3 + 2i)(2 + 3i)$

11. $(\sqrt{3} + 2i)^2$

12. What is the conjugate of $2 - 4i$?

13. What is the conjugate of $-2 - 5i$?

14. Simplify $\frac{5 + 3i}{2 + i}$

15. Simplify $\frac{8 + 3i}{3 - 2i}$

16. What is i^2 ?

17. What is i^3 ?

18. What is i^4 ?

19. What is i^5 ?

20. What is i^{4445} ?

21. Find both members of the solution set if $x^2 - 2x + 5 = 0$

22. Find both members of the solution set if $x^2 - 2x + 2 = 0$

23. Find both members of the solution set if $x^2 + 6x + 25 = 0$

24. Find both members of the solution set if $x^2 - 4x + 9 = 0$

Answers

$$\begin{aligned} \sqrt{-9} &= \sqrt{9}i = 3i \\ \sqrt{-49} &= \sqrt{49}i = 7i \\ -2\sqrt{-1} &= -2i \\ \sqrt{-\frac{4}{9}} &= \sqrt{\frac{4}{9}}i = \frac{2}{3}i \\ \sqrt{-50} + \sqrt{-32} - \sqrt{-8} &= 5\sqrt{2}i + 4\sqrt{2}i - \sqrt{2}i = 8\sqrt{2}i \\ \sqrt{9} \cdot \sqrt{-49} &= 3 \cdot 7i = 21i \\ (7 + 2i) - (4 - 3i) &= 7 + 2i - 4 + 3i = 3 + 5i \\ (3 - 2i) + (9 - 4i) &= 3 - 2i + 9 - 4i = 12 - 6i \\ 2i(3 + 5i) &= 6i + 10i^2 = 6i - 10 = -10 + 6i \\ (3 + 2i)(2 + 3i) &= 6 + 9i + 4i + 6i^2 = 6 + 13i - 6 = 13i \\ (\sqrt{3} + 2i)^2 &= 3 + 4\sqrt{3}i + 4i^2 = 3 + 4\sqrt{3}i - 4 = -1 + 4\sqrt{3}i \end{aligned}$$

$$\begin{aligned} \text{Conjugate of } 2 - 4i &= 2 + 4i \\ \text{Conjugate of } -2 - 5i &= -2 + 5i \end{aligned}$$