BC Calc Vector 3

1. (No Calc) The position of a particle at any time  $t \ge 0$  is given by  $x(t) = t^2 - 2$ ,  $y(t) = \frac{2}{3}t^3$ . (a) Find the magnitude of the velocity vector at t = 2.

(b) Set up an integral expression to find the total distance traveled by the particle from t = 0 to t = 4.

(c) Find  $\frac{dy}{dx}$  as a function of x.

(d) At what time t is the particle on the y-axis? Find the acceleration vector at this time.

- 2. (No Calc) An object moving along a curve in the xy-plane has position (x(t), y(t)) at time t with the velocity vector  $v(t) = \langle (t+1)^{-1}, 2t \rangle$ . At time t = 1, the object is at  $(\ln 2, 4)$ .
  - (a) Find the position vector.

(b) What is the speed of the particle when t = 1.

(c) Write an equation for the line tangent to the curve when t = 1.

(d) At what time  $t \ge 0$  does the line tangent to the particle at (x(t), y(t)) have a slope of 12?

(e) Write an expression that represents how far has the particle travelled from time t = 0 to t = 1.

3. (Calc OK) A particle moving along a curve in the xy-plane has position (x(t), y(t)), with  $x(t) = 2t + 3 \sin t$  and  $y(t) = t^2 + 2 \cos t$ , where  $0 \le t \le 10$ . Find the velocity vector at the time when the particle's vertical position is y = 7.

4. (Calc OK) A particle moving along a curve in the xy-plane has position (x(t), y(t)) at time t with  $\frac{dx}{dt} = 1 + \sin(t^3)$ . The derivative  $\frac{dy}{dt}$  is not explicitly given. For any time  $t, t \ge 0$ , the line tangent to the curve at (x(t), y(t)) has a slope of t + 3. Find the acceleration vector of the object at time t = 2.

- 5. An object moving along a curve in the xy-plane has position (x(t), y(t)) at time t with  $\frac{dx}{dy} = \cos(e^t)$  and  $\frac{dy}{dt} = \sin(e^t)$  for  $0 \le t \le 2$ . At time t = 1, the object is at the point (3, 2).
  - (a) Find the equation of the tangent line to the curve at the point where t = 1.

(b) Find the speed of the object at t = 1.

(c) Find the total distance traveled by the object over the time interval  $0 \leq t \leq 2.$ 

(d) Find the position of the object at time t = 2.

- 6. A particle moving along a curve in the xy-plane has position (x(t), y(t)) at time t with  $\frac{dx}{dt} = \sin(t^3 t)$ and  $\frac{dy}{dt} = \cos(t^3 - t)$ . At time t = 3, the particle is at the point (1, 4).
  - (a) Find the acceleration vector for the particle at t = 3.

(b) Find the equation of the tangent line to the curve at the point where t = 3.

(c) Find the magnitude of the velocity vector at t = 3.

(d) Find the position of the particle at time t = 2.

7. An object moving along a curve in the xy-plane has position (x(t), y(t)) at time t with dy/dt = 2 + sin(e<sup>t</sup>). The derivative dx/dt is not explicitly given. At t = 3, the object is at the point (4,5).
(a) Find the y-coordinate of the position at time t = 1.

(b) At time t = 3, the value of  $\frac{dy}{dx}$  is -1.8. Find the value of  $\frac{dx}{dt}$  when t = 3.

(c) Find the speed of the object at time t = 3.