

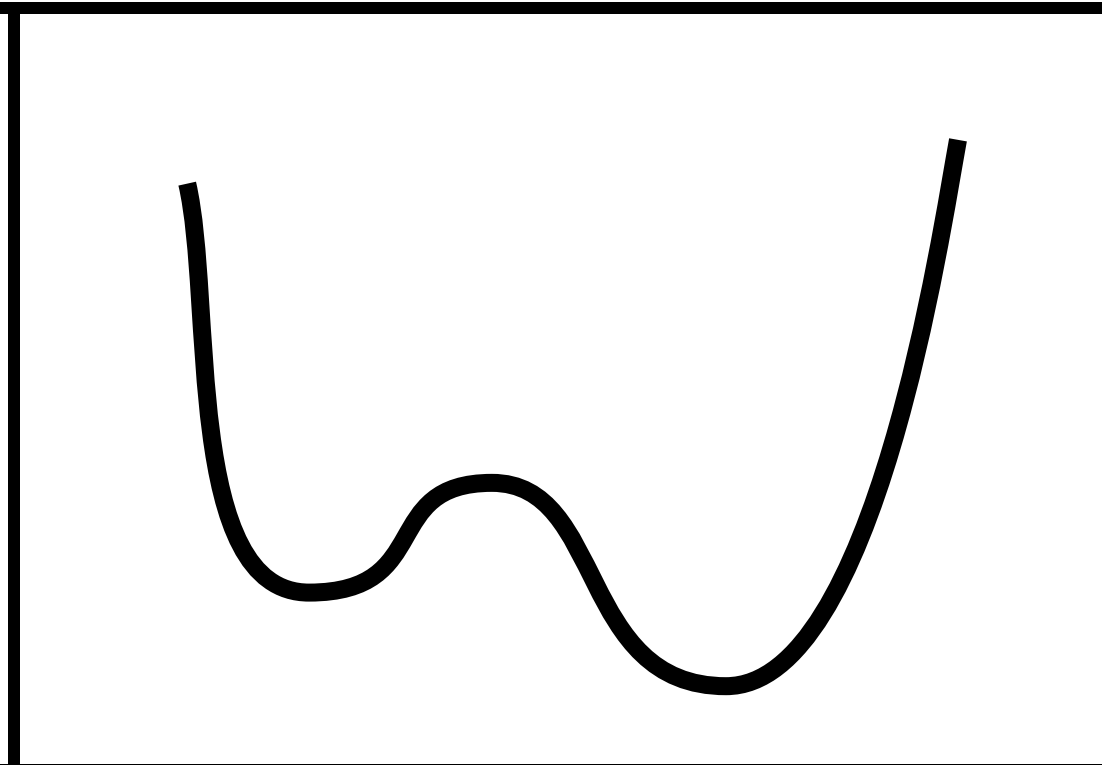
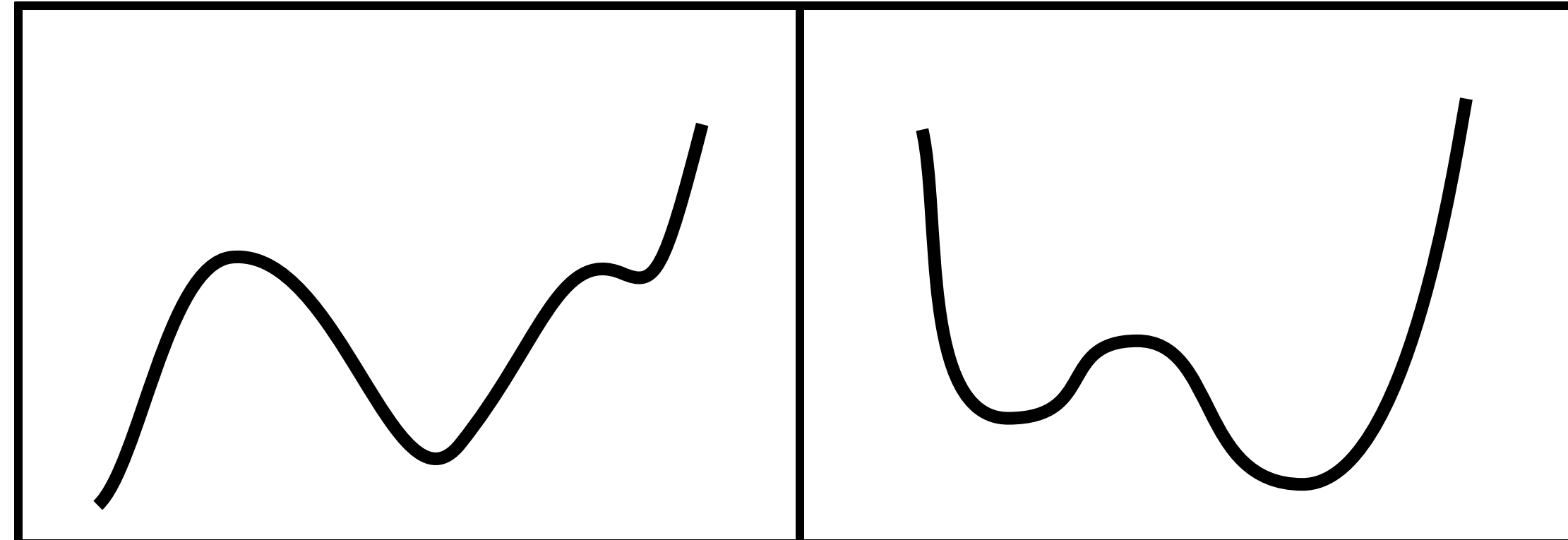
Summary of Analysis

Polynomial End Behavior

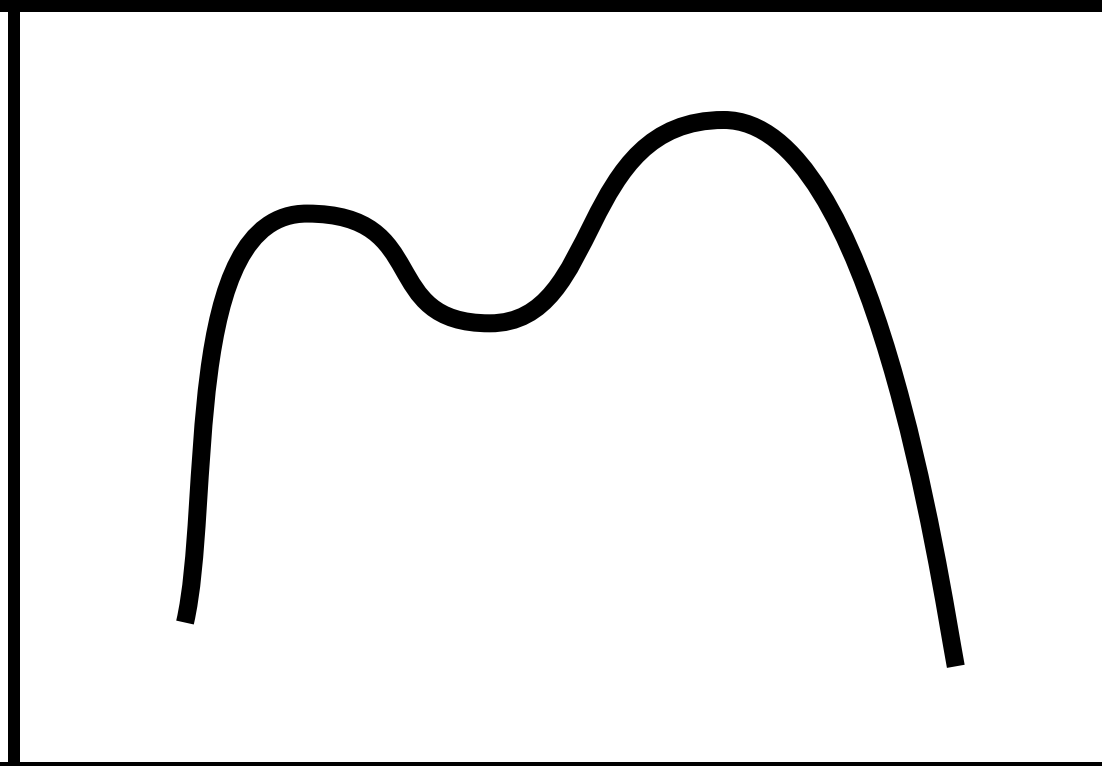
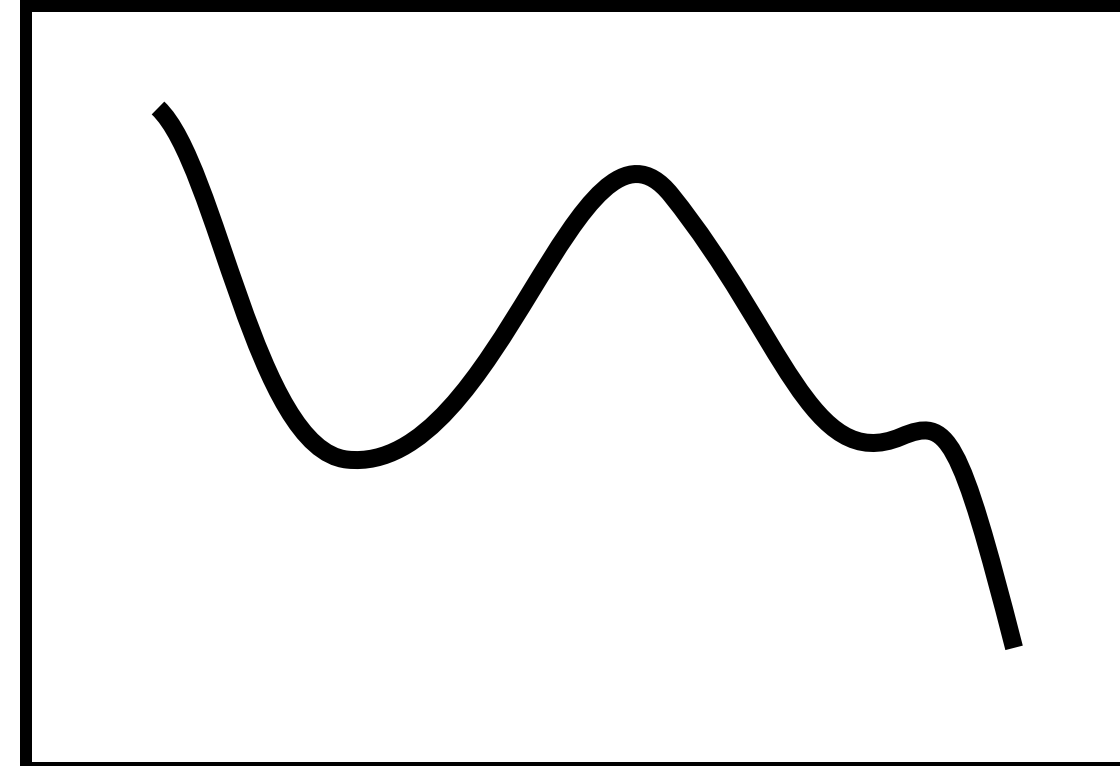
odd degree

even degree

positive leading term



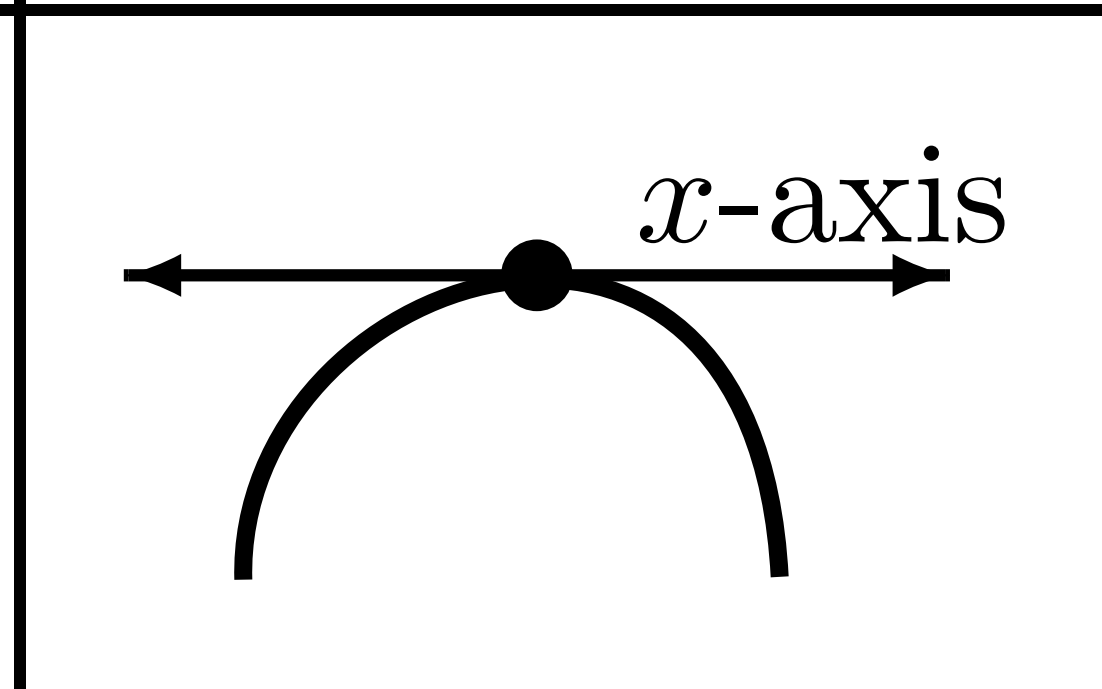
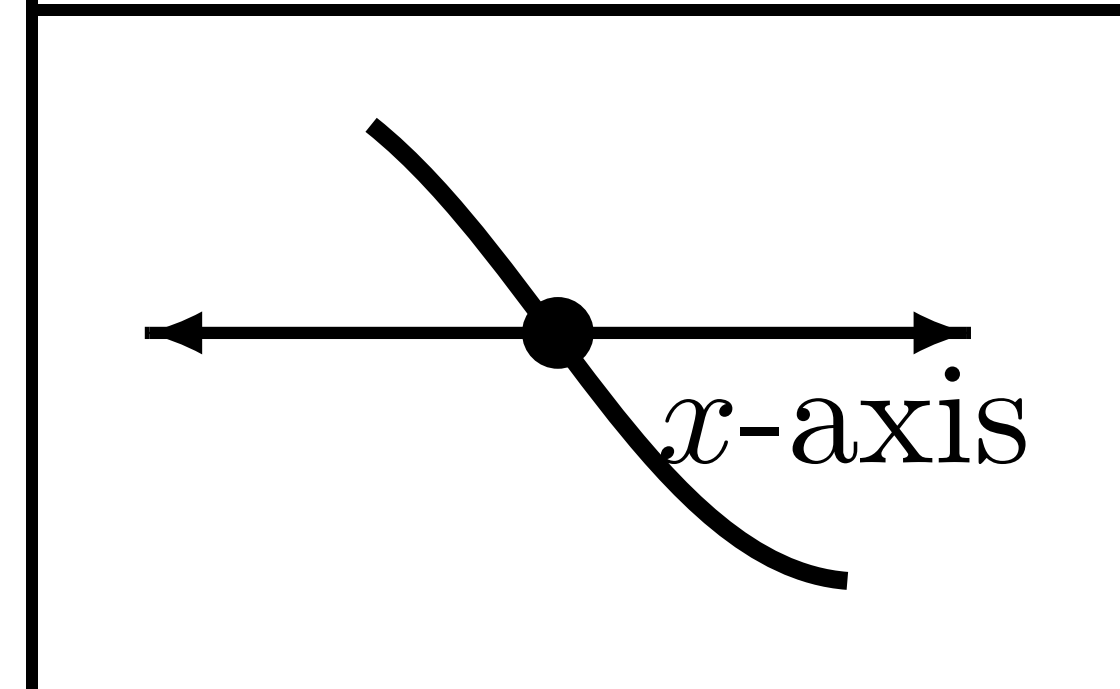
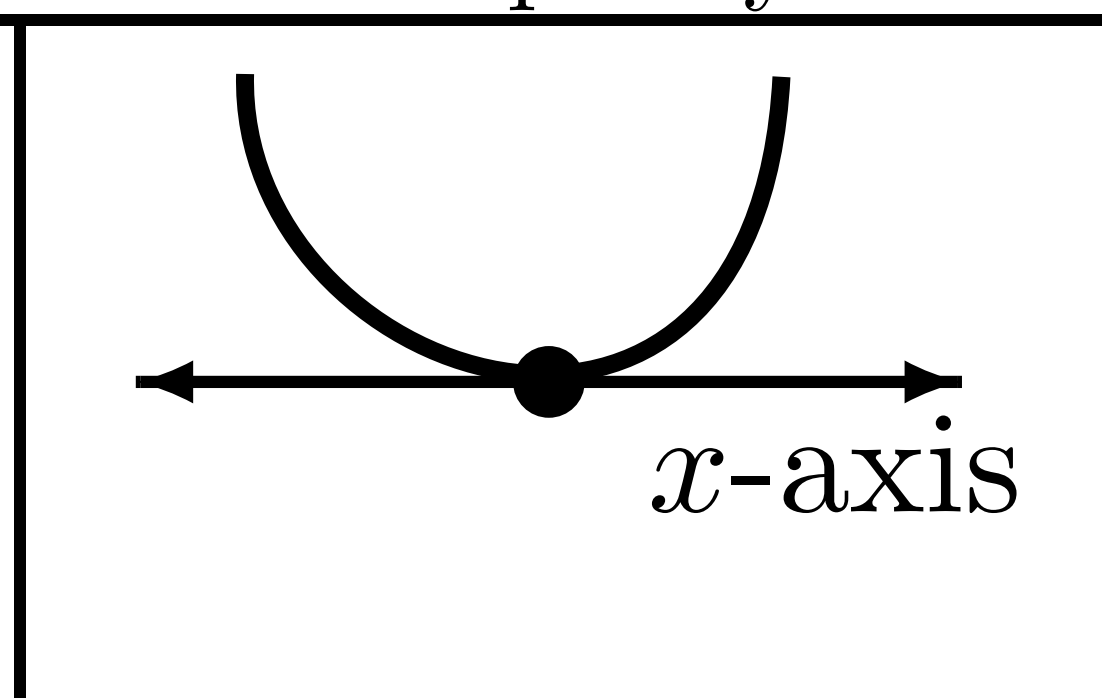
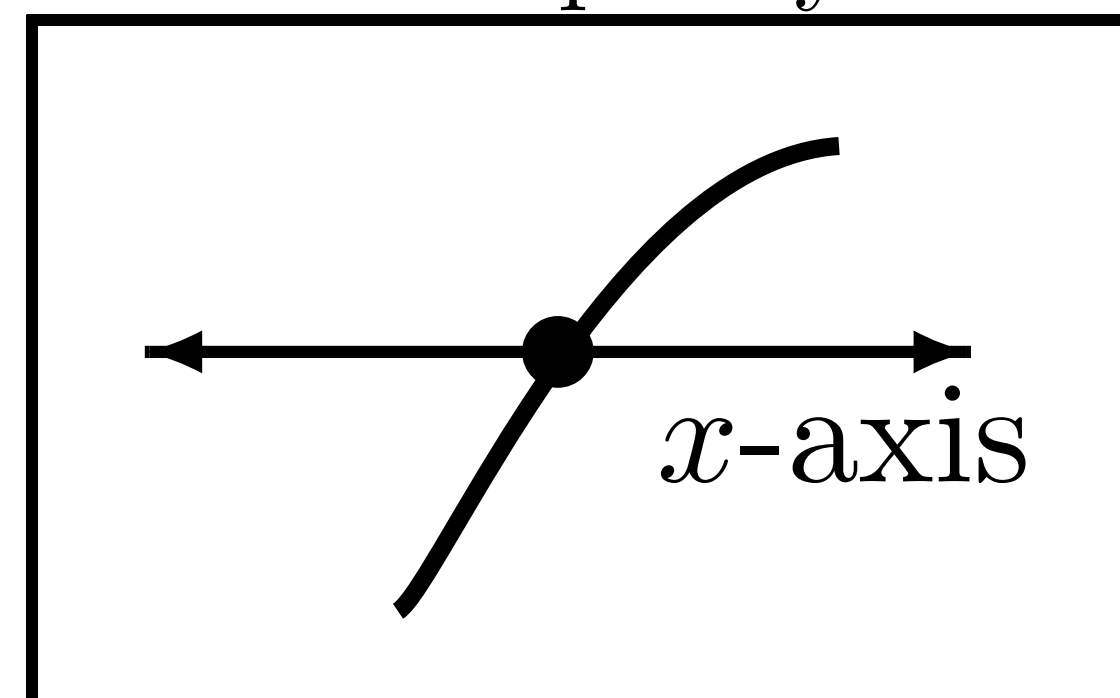
negative leading term



x -intercept behavior

zero has odd multiplicity

zero has even multiplicity



Rational End Behavior

$$R(x) = \frac{p(x)}{q(x)} = \frac{a_n x^n + a_{n-1} x^{n-1} + \dots + a_1 x + a_0}{b_m x^m + b_{m-1} x^{m-1} + \dots + b_1 x + b_0}$$

n = degree of top polynomial

m = degree of bottom polynomial

case

as $x \rightarrow \pm\infty$

$n < m$	$f(x) \rightarrow y = 0$
$n = m$	$f(x) \rightarrow y = \frac{a_n}{b_m}$
$n > m$	$f(x) \rightarrow q(x) \mid \overline{p(x)}$ (divide, ignore remainder)

3 zeros of Rational Functions

$R(0)$	y intercept
All real x that make top $p(x) = 0$	x intercepts
All real x that make bottom $q(x) = 0$	vertical asymptotes