

| l'Hôpital's Rule <br> If $\frac{f(a)}{g(b)}=\frac{0}{0}$ or $=\frac{\infty}{\infty}$, | Slope of a Parametric equation Given a $x(t)$ and a $y(t)$ the slope is | Fun | $\begin{aligned} & \text { les of } \\ & \text { ns for } \end{aligned}$ | $\begin{aligned} & \text { onom } \\ & \text { mmol } \end{aligned}$ | $\begin{aligned} & \text { ic } \\ & \text { ngles } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\theta$ | $\sin \theta$ | $\cos \theta$ | $\tan \theta$ |
| then $\lim _{x \rightarrow a} \frac{f(x)}{g(x)}=\lim _{x \rightarrow a} \frac{f(x)}{g^{\prime}(x)}$ |  | $0^{\circ}$ | 0 | 1 | 0 |
| Euler's Method If given that $\frac{d y}{d x}$ and that the | Polar Curve <br> For a polar curve $r(\theta)$, the AREA inside a "leaf" is | $\frac{\pi}{6}, 30^{\circ}$ | $\frac{1}{2}$ | $\frac{\sqrt{3}}{2}$ | $\frac{\sqrt{3}}{3}$ |
| solution passes through $\left(x_{o}, y_{o}\right)$, | $\int_{\theta_{1}}^{\theta_{2}} \frac{1}{2}[r(\theta)]^{2} d \theta$ | $\frac{\pi}{4}, 45^{\circ}$ | $\frac{\sqrt{2}}{2}$ | $\frac{\sqrt{2}}{2}$ | 1 |
| - Use a tangent line to build | that $r=0$. | $53^{\circ}$ | 4/5 | 3/5 | 4/3 |
| $y=y_{1}+\frac{d y}{d x}\left(x-x_{1}\right)$ | The SLOPE of $r(\theta)$ at a given $\theta$ is $x=r \cos \theta \quad y=r \operatorname{sins} \theta$ | $\frac{\pi}{3}, 60^{\circ}$ | $\frac{\sqrt{3}}{2}$ | $\frac{1}{2}$ | $\sqrt{3}$ |
|  | $\frac{\mathrm{dy}}{\mathrm{dy}}=\frac{d y / d \theta}{d x /}$ | $\frac{\pi}{2}, 90^{\circ}$ | 1 | 0 | " $\infty$ " |
|  | $\mathrm{dx} \quad d x / d \theta$ | $\pi, 180^{\circ}$ | 0 | -1 | 0 |
| Tabular Integration - When one piece is not the derivative of the other $\int \ln x d x=$ | Ratio Test <br> The series $\sum_{k=0}^{\infty} a_{k}$ converges if | L'hopit <br> a functi | $\begin{gathered} \hline \text { Rule: } \\ \text { is } \frac{0}{n} \end{gathered}$ |  | mit of |
|  |  |  | $0$ | $\alpha$ |  |
| 1/x $\quad \mathbf{x}$ | $a_{k}$ | Take th | tiv | op |  |
| $\begin{aligned} & \int \ln x d x=x \ln x-\int 1 d x \\ & \int \ln x d x=x \ln x-x+C \end{aligned}$ | If the limit equal 1 , you know nothing. <br> Interval of convergence (Test endpoints) | derivative re-evalua |  |  |  |
| Taylor Series <br> If the function $f$ is "smooth" at $x=a$, then it can be approximated by the $n^{\text {th }}$ degree polynomial $\begin{aligned} f(x) \approx f(a) & +f^{\prime}(a)(x-a) \\ & +\frac{f^{\prime \prime}(a)}{2!}(x-a)^{2}+\ldots \\ & +\frac{f^{(n)}(a)}{n!}(x-a)^{n} . \end{aligned}$ <br> Take derivatives, plug in your center and divide by your factorials. | Lagrange Error Bound If $P_{n}(x)$ is the $n^{\text {th }}$ degree Taylor polynomial of $f(x)$ about $c$ and $\left\|f^{(n+1)}(t)\right\| \leq M$ for all $t$ between $x$ and $c$, then $\left\|f(x)-P_{n}(x)\right\| \leq \frac{M}{(n+1)!}\|x-c\|^{n+1}$ <br> $\mathrm{M}=$ Maximum of the next derivative ( $\mathrm{x}-\mathrm{c}$ ) is the distance from center $(\mathrm{n}+1)$ ! Is the next derivative $\left\|f(x)-P_{n}(x)\right\|$ is the actual error | Sum of $S=\frac{1^{s t} t}{1}$ <br> where $r$ | finite <br> he con | metric <br> ratio |  |
| Maclaurin Series <br> A Taylor Series about $x=0$ is called Maclaurin. $\begin{aligned} e^{x} & =1+x+\frac{x^{2}}{2!}+\frac{x^{3}}{3!}+\ldots \\ \cos x & =1-\frac{x^{2}}{2!}+\frac{x^{4}}{4!}-\ldots \\ \sin x & =x-\frac{x^{3}}{3!}+\frac{x^{5}}{5!}-\ldots \\ \frac{1}{1-x} & =1+x+x^{2}+x^{3}+\ldots \\ \ln (x+1) & =x-\frac{x^{2}}{2}+\frac{x^{3}}{3}-\frac{x^{4}}{4}+\ldots \end{aligned}$ | Alternating Series Error Bound <br> If $S_{N}=\sum_{k=1}^{N}(-1)^{n} a_{n}$ is the $N^{\text {th }}$ partial sum of a convergent alternating series, then $\left\|S_{\infty}-S_{N}\right\| \leq\left\|a_{N+1}\right\|$ <br> This means error is less than the next term <br> Integration by Separation <br> Don't forget +C <br> Get y with dy and x with dx |  |  |  |  |

