

Ch 4 MC Practice**Multiple Choice***Identify the choice that best completes the statement or answers the question.*

- ____ 1. Find the general solution of the differential equation below and check the result by differentiation.

$$\frac{dQ}{du} = -24u^7$$

- a. $Q(u) = -3u^8 + 1$
- b. $Q(u) = -3u^8$
- c. $Q(u) = -168u^6$
- d. $Q(u) = -3u^8 + C$
- e. $Q(u) = -168u^6 + C$

- ____ 2. Find the indefinite integral $\int (-8t + 7)dt$.

- a. $-8t^2 + 7t + C$
- b. $-4t^2 + 7t$
- c. $-4t^2 + 7t + C$
- d. -8
- e. none of the above

- ____ 3. Find the indefinite integral $\int \sqrt[13]{x^8} dx$.

- a. $\frac{8}{13}x^{21} + C$
- b. $\frac{21}{13}x^{13/21} + C$
- c. $\frac{8}{21}x^{8/21} + C$
- d. $\frac{13}{8}x^{21} + C$
- e. $\frac{13}{21}x^{21/13} + C$

- ____ 4. Find the indefinite integral and check the result by differentiation.

$$\int \frac{3z^2 + 12z - 9}{z^4} dz$$

- a. $-\frac{3}{z} + \frac{12}{z^2} + \frac{9}{z^3} + C$
- b. $-\frac{3}{z} - \frac{6}{z^2} + \frac{3}{z^3}$
- c. $\frac{3}{z} - \frac{6}{z^2} + \frac{3}{z^3} + C$
- d. $-\frac{3}{z} + \frac{6}{z^2} + \frac{3}{z^3}$
- e. $-\frac{3}{z} - \frac{6}{z^2} + \frac{3}{z^3} + C$

- ____ 5. An evergreen nursery usually sells a certain shrub after 4 years of growth and shaping. The growth rate during those 4 years is approximated by $\frac{dh}{dt} = 2.5t + 6$, where t is the time in years and h is the height in centimeters. The seedlings are 15 centimeters tall when planted ($t = 0$). Find the height after t years.

- a. $h(t) = 1.25t^2 + 21t$
- b. $h(t) = 1.25t^2 + 6t + 15$
- c. $h(t) = 1.25t + 15$
- d. $h(t) = 2.5t^2 + 6t + 15$
- e. $h(t) = 2.5t + 21$

- ____ 6. A ball is thrown vertically upwards from a height of 5 ft with an initial velocity of 40 ft per second. How high will the ball go? Note that the acceleration of the ball is given by $a(t) = -32$ feet per second per second.

- a. 23.7500 ft
- b. 30.0000 ft
- c. 70.0000 ft
- d. 80.8000 ft
- e. 80.0000 ft

- ____ 7. The maker of an automobile advertises that it takes 12 seconds to accelerate from 30 kilometers per hour to 85 kilometers per hour. Assuming constant acceleration, compute the acceleration in meters per second per second. Round your answer to three decimal places.

- a. 1.528 m/sec²
- b. 2.662 m/sec²
- c. 2.865 m/sec²
- d. 3.194 m/sec²
- e. 1.273 m/sec²

- ____ 8. Use left endpoints and 10 rectangles to find the approximation of the area of the region between the graph of the function $4x^2 - x - 1$ and the x -axis over the interval $[4, 14]$. Round your answer to the nearest integer.
- a. 2925
b. 3325
c. 3000
d. 3250
e. 3125
- ____ 9. Find the limit.

$$\lim_{n \rightarrow \infty} \sum_{i=1}^n \left(\frac{10i}{n} \right) \left(\frac{8}{n} \right)$$

- a. 20
b. 18
c. 36
d. 80
e. 40

- ____ 10. Write the following limit as a definite integral on the interval $[2, 5]$, where c_i is any point in the i th subinterval.

$$\lim_{|\Delta x| \rightarrow 0} \sum_{i=1}^n (-7c_i + 2)\Delta x_i$$

a. $\int_2^5 (-7x^2 + 2x)dx$

b. $\int_2^5 \left(-\frac{7}{2}x^2 - 2x\right)dx$

c. $\int_2^5 (-7x + 2)dx$

d. $\int_5^2 (-7x + 2)dx$

e. $\int_2^5 (-7x - 2)dx$

- ____ 11. Write the limit $\lim_{|\Delta x| \rightarrow 0} \sum_{i=1}^n 4c_i(7-c_i)^2 \Delta x_i$, as a definite integral on the interval $[0, 8]$ where c_i is any point in the i^{th} subinterval.

a. $\int 4x(7-x)^8 dx$

b. $\int_8^0 4x^2(7-x)^8 dx$

c. $\int 4c_i(7-c_i)^2 \Delta x_i$

d. $\int_0^8 4x(7-x)^2 dx$

e. $\int_0^{c_i} 4c_i(7-c_i)^2 \Delta x_i$

- ____ 12. Write the limit $\lim_{|\Delta| \rightarrow 0} \sum_{i=1}^n \left(\frac{6}{c_i^2} \right) \Delta x_i$, as a definite integral on the interval $[8, 10]$, where c_i is any point in the i^{th} subinterval.

a. $\int_{10}^8 \frac{6}{x^2} dx$

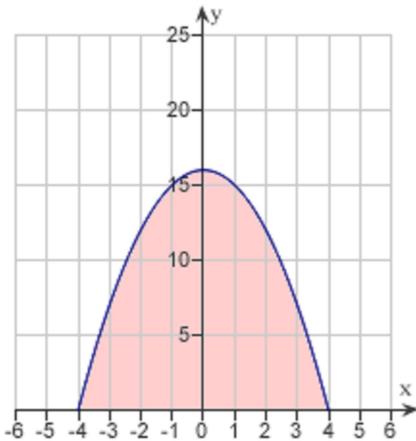
b. $\int_0^8 \frac{6}{x^2} dx$

c. $\int_0^2 \frac{6}{x^2} dx$

d. $\int_0^{10} \frac{6}{x^2} dx$

e. $\int_8^{10} \frac{6}{x^2} dx$

13. The graph of the function $f(x) = 16 - x^2$ is given below. Which of the following definite integrals yields the area of the shaded region?



a. $\int_0^{16} (16 - x^2) dx$

b. $\int_{-4}^0 (16 - x^2) dx$

c. $\int_0^4 (16 - x^2) dx$

d. $\int_{-16}^{16} (16 - x^2) dx$

e. $\int_{-4}^4 (16 - x^2) dx$

- ____ 14. Sketch the region whose area is given by the definite integral and then use a geometric formula to evaluate the integral.

$$\int_{1}^{4} 2s \, ds$$

- a. 30
- b. 15
- c. 4
- d. 34
- e. -17

- ____ 15. Sketch the region whose area is given by the definite integral and then use a geometric formula to evaluate the integral.

$$\int_{0}^{5} (6t + 1) \, dt$$

- a. -158
- b. 12
- c. 80
- d. 82
- e. -160

- ____ 16. Sketch the region whose area is given by the definite integral and then use a geometric formula to evaluate the integral.

$$\int_{-1}^{1} (1 - |u|) \, du$$

- a. -1
- b. 1
- c. 2
- d. 4
- e. 15

____ 17. Evaluate the integral.

$$\int_{-7}^6 -24x \, dx$$

given,

$$\int_6^7 x^3 \, dx = \frac{1105}{4},$$

$$\int_6^7 x^2 \, dx = \frac{127}{3},$$

$$\int_6^7 x \, dx = \frac{13}{2},$$

$$\int_6^7 dx = 1.$$

- a. -156
- b. 156
- c. 1,016
- d. 24
- e. 6,630

____ 18. Evaluate the integral.

$$\int_5^6 (-12u^3 - 2u) du$$

given,

$$\int_5^6 x^3 dx = \frac{671}{4},$$

$$\int_5^6 x^2 dx = \frac{91}{3},$$

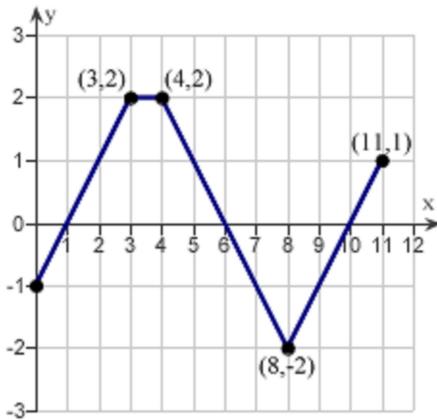
$$\int_5^6 x dx = \frac{11}{2},$$

$$\int_5^6 dx = 1.$$

- a. -65
- b. -2377
- c. -66
- d. -2024
- e. -2025

11

- ____ 19. The graph of f consists of line segments, as shown in the figure. Evaluate the definite integral $\int_0^{11} f(x)dx$ using geometric formulas.



- a. 4
b. 3
c. 1
d. 2
e. 5
- ____ 20. Evaluate the definite integral of the algebraic function.

$$\int_3^6 (5u + 4)du$$

3

Use a graphing utility to verify your results.

- a. 148.5
b. 12
c. 79.5
d. 159
e. 15

____ 21. Evaluate the definite integral $\int_2^4 \frac{6}{u^3} du$. Use a graphing utility to verify your results.

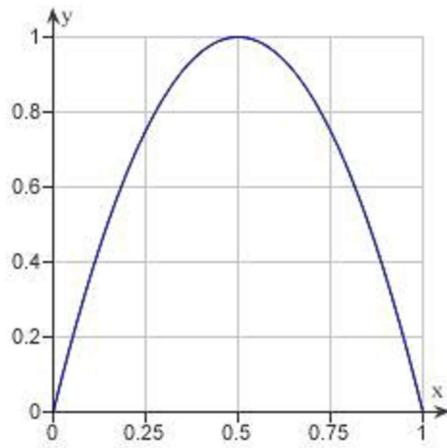
- a. $\frac{9}{8}$
- b. $\frac{3}{8}$
- c. $\frac{3}{32}$
- d. $\frac{1}{16}$
- e. $\frac{9}{16}$

____ 22. Evaluate the definite integral of a function $\int_0^1 u^{\frac{3}{2}} du$. Use a graphing utility to verify your results.

- a. $\frac{3}{4}$
- b. $\frac{9}{7}$
- c. $\frac{7}{8}$
- d. $\frac{2}{5}$
- e. $\frac{5}{6}$

_____ 23. Determine the area of the given region.

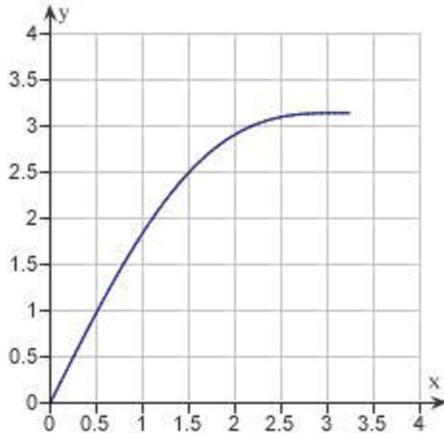
$$y = 4x(1 - x)$$



- a. $\frac{3}{7}$
- b. $\frac{2}{5}$
- c. $\frac{2}{3}$
- d. $\frac{2}{9}$
- e. $\frac{10}{3}$

- _____ 24. Determine the area of the given region.

$$y = x + \sin x, 0 \leq x \leq \pi$$



- a. $0.5\pi^2 + 2$
b. $2\pi^2 + 1$
c. $0.5\pi^2 + 5$
d. $0.5\pi^2 + 3$
e. $0.5\pi^2 + 1$
- _____ 25. Find the average value of the function $f(x) = 48 - 12x^2$ over the interval $-5 \leq x \leq 5$.

- a. -152
b. -52
c. 148
d. 248
e. -252

- ____ 26. Find the average value of the function over the given interval and all values t in the interval for which the function equals its average value.

$$f(t) = \frac{t^2 + 4}{t^2}, \quad 1 \leq t \leq 5$$

Use a graphing utility to verify your results.

- a. The average is $\frac{9}{5}$ and the point at which the function is equal to its mean value is $\sqrt{5}$.
- b. The average is $\frac{9}{5}$ and the point at which the function is equal to its mean value is $\sqrt{5}$ and $-\sqrt{5}$.
- c. The average is $\frac{9}{20}$ and the point at which the function is equal to its mean value is $-\sqrt{5}$.
- d. The average is $\frac{9}{20}$ and the point at which the function is equal to its mean value is $\sqrt{5}$.
- e. The average is $\frac{9}{20}$ and the point at which the function is equal to its mean value is $\sqrt{5}$ and $-\sqrt{5}$.

- ____ 27. Find the average value of $f(x) = \frac{5(x^2 + 5)}{x^2}$ on the interval $[1, 3]$.

- a. $\frac{40}{3}$
- b. 35
- c. $\frac{25}{3}$
- d. $\frac{80}{3}$
- e. 40

- ____ 28. The volume V in liters of air in the lungs during a five-second respiratory cycle is approximated by the model $V = 0.1724t + 0.1523t^2 - 0.0377t^3$ where t is the time in seconds. Approximate the average volume of air in the lungs during one cycle. Round your answer to four decimal places.

- a. 1.8776 liter
- b. 2.0094 liter
- c. 0.4004 liter
- d. 0.8148 liter
- e. 0.5220 liter

- ____ 29. Find $F'(x)$ given

$$F(x) = \int_x^{x+3} (10t + 1) dt.$$

- a. $F'(x) = 1 + 10t$
- b. $F'(x) = 1 + 10x$
- c. $F'(x) = 30$
- d. $F'(x) = 48 + 30x^2$
- e. $F'(x) = 48 + 30t$

- ____ 30. Find $F'(x)$ given

$$F(x) = \int_{-2x}^{2x} s^2 ds.$$

- a. $F'(x) = 16x^2$
- b. $F'(x) = 4x^2$
- c. $F'(x) = 8x^2$
- d. $F'(x) = 0$
- e. $F'(x) = 24x^2$

____ 31. Find the indefinite integral $\int (1+4t)^3 dt.$

a. $\frac{(1+4t)^4}{12} + C$

b. $4(1+4t)^4 + C$

c. $\frac{(1+4t)^4}{4} + C$

d. $\frac{(1+4t)^4}{3} + C$

e. $\frac{(1+4t)^4}{16} + C$

____ 32. Find the indefinite integral $\int t^4 (4+t^5)^3 dt.$

a. $\frac{(4+t^5)^4}{4} + C$

b. $\frac{(4+t^5)^4}{20} + C$

c. $20(4+t^5)^4 + C$

d. $\frac{(4+t^4)^4}{20} + C$

e. $\frac{(4+t^5)^4}{10} + C$

____ 33. Find the indefinite integral $\int z^3 \sqrt{2+z^4} dz$.

a. $\frac{(2+z^4)^{\frac{3}{2}}}{8} + C$

b. $\frac{2(2+z^4)^{\frac{3}{2}}}{12} + C$

c. $\frac{(2+z^4)^{\frac{3}{2}}}{12} + C$

d. $\frac{2(2+z^4)^{\frac{2}{3}}}{12} + C$

e. $\frac{2(2+z^4)^{\frac{5}{2}}}{20} + C$

____ 34. Find the indefinite integral of the following function and check the result by differentiation.

$$\int \frac{6t^5}{t^6 + 1} dt$$

a. $\frac{1}{2} \sqrt{t^6 + 1} + C$

b. $2\sqrt{t^6 + 1} + C$

c. $\frac{1}{2} \sqrt{t^5 + 1} + C$

d. $\sqrt{t^6 + 1} + C$

e. $2\sqrt{t^5 + 1} + C$

____ 35. Solve the differential equation.

$$\frac{df}{dx} = 16x + \frac{5x}{\sqrt{9-x^2}}$$

- a. $f(x) = 8x^2 - 5\sqrt{9-x^2} + C$
- b. $f(x) = 8x^2 - \frac{5}{2}\sqrt{9-x^2} + C$
- c. $f(x) = 8x - 5\sqrt{9-x^2} + C$
- d. $f(x) = 8x^2 + 5\sqrt{9-x^2} + C$
- e. $f(x) = 8x^2 - \frac{5}{\sqrt{9-x^2}} + C$

____ 36. Find the indefinite integral of the following function.

$$\int \cos 2s \, ds$$

- a. $\cos 2s + C$
- b. $\sin 2s + C$
- c. $\frac{\sin 2s}{3} + C$
- d. $2 \sin 2s + C$
- e. $\frac{\sin 2s}{2} + C$

____ 37. Find the indefinite integral $\int 7x^6 \sin x^7 \, dx$.

- a. $\frac{-\cos x^8}{8} + C$
- b. $\sin x^7 + C$
- c. $-\cos x^7 + C$
- d. $-\cos x^6 + C$
- e. $\frac{-\cos x^7}{7} + C$

____ 38. Find the indefinite integral of the following function.

$$\int \frac{\sin u}{\cos^3 u} du$$

- a. $\frac{(\cos u)^{-2}}{2} + C$
- b. $\frac{(\sin u)^{-2}}{3} + C$
- c. $\frac{(\cos u)^{-3}}{2} + C$
- d. $\frac{(\cos u)^{-2}}{3} + C$
- e. $\frac{(\sin u)^{-2}}{2} + C$

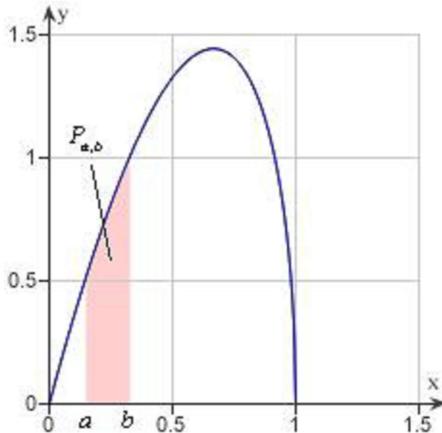
____ 39. Evaluate the following definite integral.

$$\int_1^4 \frac{1}{\sqrt{4u+7}} du$$

Use a graphing utility to check your answer.

- a. $\frac{\sqrt{23} + \sqrt{11}}{4}$
- b. $\frac{\sqrt{11} - \sqrt{23}}{2}$
- c. $\frac{\sqrt{23} + \sqrt{11}}{2}$
- d. $\frac{\sqrt{23} - \sqrt{11}}{4}$
- e. $\frac{\sqrt{23} - \sqrt{11}}{2}$

40. The sales S (in thousands of units) of a seasonal product are given by the model $S = 73.36 + 45.74 \sin \frac{\pi t}{6}$ where t is the time in months, with $t = 1$ corresponding to January. Find the average sales for the first quarter ($0 \leq t \leq 3$). Round your answer to three decimal places.
- a. 131.598 thousand units
b. 92.442 thousand units
c. 74.859 thousand units
d. 102.479 thousand units
e. 92.924 thousand units
41. The oscillating current in an electrical circuit is $I = 2 \sin(60\pi t) + \cos(120\pi t)$ where I is measured in amperes and t is measured in seconds. Find the average current for the time interval $0 \leq t \leq \frac{1}{60}$. Round your answer to three decimal places.
- a. 2.273 amps
b. 1.273 amps
c. 0.637 amps
d. 2.546 amps
e. 1.637 amps
42. Suppose that the probability that a person will remember between $100a\%$ and $100b\%$ of material learned in an experiment is $P_{a,b} = \int_a^b \frac{15}{4} x \sqrt{1-x} dx$ where x represents the proportion remembered. Determine from the figure below, the probability that a randomly chosen individual will recall between 50% and 55% of the material? Express your answer as a percent rounded to three decimal places.



- a. 39.000%
b. 6.800%
c. 1.600%
d. 47.800%
e. 85.300%

Ch 4 MC Practice

Answer Section

MULTIPLE CHOICE

1. ANS: D PTS: 1 DIF: Easy
OBJ: Calculate the general solution of a differential equation
REF: Section 4.1
MSC: Skill
2. ANS: C PTS: 1 DIF: Easy
OBJ: Evaluate the indefinite integral of a function
REF: Section 4.1
MSC: Skill
3. ANS: E PTS: 1 DIF: Easy
OBJ: Evaluate the indefinite integral of a function
REF: Section 4.1
MSC: Skill
4. ANS: E PTS: 1 DIF: Medium
OBJ: Evaluate the indefinite integral of a function
REF: Section 4.1
MSC: Skill
5. ANS: B PTS: 1 DIF: Easy
OBJ: Solve a differential equation in applications
REF: Section 4.1
MSC: Application
6. ANS: B PTS: 1 DIF: Medium
OBJ: Solve differential equations related to position/velocity/acceleration
MSC: Application
REF: Section 4.1
7. ANS: E PTS: 1 DIF: Medium
OBJ: Calculate the acceleration
MSC: Application
REF: Section 4.1
8. ANS: E PTS: 1 DIF: Medium
OBJ: Approximate the area bounded by a function using rectangles
MSC: Skill
REF: Section 4.2
9. ANS: E PTS: 1 DIF: Medium
OBJ: Evaluate an infinite limit of a sum
MSC: Skill
REF: Section 4.2
10. ANS: C PTS: 1 DIF: Easy
OBJ: Evaluate a definite integral by the limit definition
REF: Section 4.3
MSC: Skill
11. ANS: D PTS: 1 DIF: Easy
OBJ: Write a limit as a definite integral on an interval
REF: Section 4.3
MSC: Skill
12. ANS: E PTS: 1 DIF: Easy
OBJ: Write a limit as a definite integral on an interval
REF: Section 4.3
MSC: Skill
13. ANS: E PTS: 1 DIF: Easy
OBJ: Write a definite integral for a bounded region
REF: Section 4.3
MSC: Skill
14. ANS: B PTS: 1 DIF: Easy
OBJ: Evaluate a definite integral geometrically
REF: Section 4.3
MSC: Skill
15. ANS: C PTS: 1 DIF: Easy
OBJ: Evaluate a definite integral geometrically
REF: Section 4.3
MSC: Skill
16. ANS: B PTS: 1 DIF: Easy
OBJ: Evaluate a definite integral geometrically
REF: Section 4.3
MSC: Skill
17. ANS: B PTS: 1 DIF: Easy
OBJ: Evaluate the definite integral of a function
REF: Section 4.3
MSC: Skill
18. ANS: D PTS: 1 DIF: Easy
OBJ: Evaluate the definite integral of a function
REF: Section 4.3
MSC: Skill
19. ANS: D PTS: 1 DIF: Medium
OBJ: Evaluate a definite integral geometrically
REF: Section 4.3
MSC: Skill

20. ANS: C PTS: 1 DIF: Medium REF: Section 4.4
 OBJ: Evaluate the definite integral of a function MSC: Skill
21. ANS: E PTS: 1 DIF: Easy REF: Section 4.4
 OBJ: Evaluate the definite integral of a function MSC: Skill
22. ANS: D PTS: 1 DIF: Medium REF: Section 4.4
 OBJ: Evaluate the definite integral of a function MSC: Skill
23. ANS: C PTS: 1 DIF: Medium REF: Section 4.4
 OBJ: Calculate the area bounded by a function MSC: Application
24. ANS: A PTS: 1 DIF: Medium REF: Section 4.4
 OBJ: Calculate the area bounded by a function MSC: Application
25. ANS: B PTS: 1 DIF: Easy REF: Section 4.4
 OBJ: Calculate the average value of a function over a given interval
 MSC: Skill
26. ANS: A PTS: 1 DIF: Medium REF: Section 4.4
 OBJ: Calculate the average value of a function over a given interval and identify the point at which it occurs
 MSC: Skill
27. ANS: A PTS: 1 DIF: Easy REF: Section 4.4
 OBJ: Calculate the average value of a function over a given interval
 MSC: Skill
28. ANS: E PTS: 1 DIF: Medium REF: Section 4.4
 OBJ: Calculate the average value of a function in applications MSC: Application
29. ANS: C PTS: 1 DIF: Medium REF: Section 4.4
 OBJ: Calculate the derivative of an integral using the Second Fundamental Theorem of Calculus
 MSC: Skill
30. ANS: A PTS: 1 DIF: Medium REF: Section 4.4
 OBJ: Calculate the derivative of an integral using the Second Fundamental Theorem of Calculus
 MSC: Skill
31. ANS: E PTS: 1 DIF: Easy REF: Section 4.5
 OBJ: Evaluate the indefinite integral of a function using substitution
 MSC: Skill
32. ANS: B PTS: 1 DIF: Easy REF: Section 4.5
 OBJ: Evaluate the indefinite integral of a function using substitution
 MSC: Skill
33. ANS: B PTS: 1 DIF: Medium REF: Section 4.5
 OBJ: Evaluate the indefinite integral of a function using substitution
 MSC: Skill
34. ANS: B PTS: 1 DIF: Medium REF: Section 4.5
 OBJ: Evaluate the indefinite integral of a function using substitution
 MSC: Skill
35. ANS: A PTS: 1 DIF: Medium REF: Section 4.5
 OBJ: Solve a differential equation MSC: Skill
36. ANS: E PTS: 1 DIF: Easy REF: Section 4.5
 OBJ: Evaluate the indefinite integral of a function using substitution
 MSC: Skill
37. ANS: C PTS: 1 DIF: Easy REF: Section 4.5
 OBJ: Evaluate the indefinite integral of a function using substitution
 MSC: Skill

38. ANS: A PTS: 1 DIF: Medium REF: Section 4.5
OBJ: Evaluate the indefinite integral of a function using substitution
MSC: Skill
39. ANS: E PTS: 1 DIF: Medium REF: Section 4.5
OBJ: Evaluate the definite integral of a function using substitution
MSC: Skill
40. ANS: D PTS: 1 DIF: Medium REF: Section 4.5
OBJ: Evaluate the definite integral of a function in applications
MSC: Application
41. ANS: B PTS: 1 DIF: Medium REF: Section 4.5
OBJ: Evaluate the definite integral of a function in applications
MSC: Application
42. ANS: B PTS: 1 DIF: Difficult REF: Section 4.5
OBJ: Evaluate the definite integral of a function in applications
MSC: Application