## 6.1 Notes and Examples

Slope Fields and Graphical Solutions to Differential Equations

1. (a) Finding an equation from its derivative is called "Solving a \_\_\_\_\_\_

which informally we call a "\_\_\_\_\_

- (b) Later this chapter we will use \_\_\_\_\_ methods, but sometimes this approach, though precise, proves to be difficult or impossible.
- (c) In this section we will find a solution using graphical methods. Since we have an equation for the

slope at any point, We draw short line segments with the correct \_\_\_\_\_\_ at various points.

(d) Once we have a few of these, we call it a \_\_\_\_\_ or a

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2. Here are some slope fields. What kind of equations do they look like to you?

3. Compute the slope at various points to sketch a slope field.



## 4. Match the "diffEQ" with its slope field

(a) 
$$\frac{dy}{dx} = 2y$$
  
(b) 
$$\frac{dy}{dx} = 2x$$
  
(c) 
$$\frac{dy}{dx} = x + 1$$
  
(d) 
$$\frac{dy}{dx} = y - 1$$
  
(e) 
$$\frac{dy}{dx} = x + y$$

(f) 
$$\frac{dy}{dx} = -\frac{x}{y}$$

D.
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- 5. Sketch a solution of the differential equation whose slope field is shown above that passes through the point (-1, 1)
- 6. Sketch a solution of the differential equation whose slope field is shown above that passes through the point (3,3)
- 7. Sketch a solution of the differential equation whose slope field is shown above that passes through the point (-1, -1)
- 8. Show  $y = 4e^{-6x^2}$  is a solution to the differential equation  $\frac{dy}{dx} = -12xy$  that goes through (0,4)

- 9. Delta Math Practice Slope fields https://www.deltamath.com/
- 10. 6.1 WS: Slope Fields https://www.mathorama.com/gsp/Chapter%206.1%20WS.pdf
- 11. Make your own Slope Field and find a particular solution with GeoGebra: https://www.geogebra.org/m/Pd4Hn4BR
- 12. Check your solutions at Desmos: https://www.desmos.com/calculator/tmi3vk4r84