

Are you Ready for Calculus?

1. Simplify each of the following:

a. $\frac{x^3 - 9x}{x^2 - 7x + 12}$

b. $\frac{x^2 - 2x - 8}{x^3 + x^2 - 2x}$

c. $\frac{\frac{1}{x} - \frac{1}{5}}{\frac{1}{x^2} - \frac{1}{25}}$

2. Rationalize the denominator in each expression:

a. $\frac{2}{\sqrt{3} + \sqrt{2}}$

b. $\frac{4}{1 - \sqrt{5}}$

3. Factor each expression completely:

a. $x^6 - 16x^4$

b. $4x^3 - 8x^2 - 25x + 50$

c. $8x^3 + 27$

4. Find the domain of each function:

a. $f(x) = \frac{5x - 3}{2x + 1}$

b. $f(x) = \sqrt{x - 1}$

5. Given $f(x) = \sqrt{x}$ and $g(x) = x^2 - 1$ find the composite functions:

a. $f(g(1))$

b. $g(f(0))$

c. $f(g(x))$

d. $g(f(x))$

6. Evaluate $\frac{f(x+h) - f(x)}{h}$ for the following functions:

a. $f(x) = 2x + 3$

b. $f(x) = \frac{1}{x+1}$

c. $f(x) = x^2$

7. Without using a calculator, evaluate the following:

a. $\cos 210^\circ$

b. $\sin \frac{5\pi}{4}$

c. $\cos \frac{9\pi}{4}$

d. $\tan \frac{7\pi}{6}$

e. $\sin 225^\circ$

8. Determine the quadrant in which θ lies:

a. $\sin \theta > 0$ and $\cos \theta < 0$

b. $\sec \theta > 0$ and $\cot \theta < 0$

9. Find two solutions of each equation. Express results in radians ($0 \leq \theta \leq 2\pi$). Do not use a calculator.

a. $\cos \theta = \frac{\sqrt{2}}{2}$

b. $\cos \theta = -\frac{\sqrt{3}}{2}$

c. $\tan \theta = 1$

d. $\cot \theta = \sqrt{3}$