by Pythagoras: $b^2 = c^2 - 2cp + a^2$