AP Calculus BC Quiz 2

1. (Inspired by 2004, #5, a 15 minute "No Calculator" question-feel free to use a calculator today)

A population is modeled by a function P that satisfies the logistic differential equation

$$\frac{dP}{dt} = \frac{P}{4} \left(1 - \frac{P}{18} \right).$$

(a) (2 points) If P(0) = 5, what is $\lim_{t \to \infty} P(t)$?

If P(0) = 25, what is $\lim_{t \to \infty} P(t)$?

(b) (1 point) If P(0) = 5, for what value of P is the population growing the fastest?

(c) (5 points) A different population is modeled by a function Y that satisfies the separable differential equation

$$\frac{dY}{dt} = \frac{Y}{4} \left(1 - \frac{t}{18} \right).$$

Find Y(t) is Y(0) = 5

(d) (1 point) For the function Y found in part (c), what is the $\lim_{t\to\infty} Y(t)$?

2. (2 points) (*Review*) Consider the curve given by $x^2 + 5y^2 = 9 + 2xy$. Show that $\frac{dy}{dx} = \frac{x - y}{x - 5y}$